hedral holes. Despite the low scattering power of V for neutrons, neutron diffraction was used because N has a large scattering power. Hence, in this experiment the structure was determined solely by the N atom positions. The investigation confirmed that $\beta-\mathrm{V}_{2} \mathrm{~N}$ has the $\varepsilon-\mathrm{Fe}_{2} \mathrm{~N}$ structure, similar to $\beta-\mathrm{Nb}_{2} \mathrm{~N}$ and $\beta-\mathrm{Ta}_{2} \mathrm{~N}$.

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# Structure of Dilithium Zinc Silicate $\gamma_{\mathrm{II}}-\mathrm{Li}_{\mathbf{2}} \mathbf{Z n S i O}_{4}$ 

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#### Abstract

Li}_{2} \mathrm{ZnSiO}_{4}\), monoclinic, $P 2_{1} / n, a=6.262$ (3), $b=10.602$ (4), $c=5.021$ (4) $\AA, \beta=90.51$ (5) ${ }^{\circ}, Z=$ $4, D_{x}=3.41 \mathrm{Mg} \mathrm{m}{ }^{-3}, \mu($ Mo $K a)=7.65 \mathrm{~mm}^{-1}$. Crystals were twinned on ( 001 ) with $a$ as the twin axis. The structure of the $\gamma_{\mathrm{II}}$ modification has been solved by the heavy-atom method and refined by the leastsquares method to $R=0.060$ for 772 observed reflections with the twin ratio $0 \cdot 65: 0.35$. All cations are coordinated tetrahedrally by O atoms.


Introduction. Setoguchi \& Sakamoto (1974) and Setoguchi (1979) have synthesized the compounds $\mathrm{Li}_{2} M^{2+} \mathrm{SiO}_{4}(M=\mathrm{Zn}, \mathrm{Mg})$ by a flux method. In this paper we deal with the structure determination of $\gamma_{\mathrm{II}^{-}}$ $\mathrm{Li}_{2} \mathrm{ZnSiO}_{4}$ as part of a systematic study of these compounds.
Crystals of $\gamma_{11}-\mathrm{Li}_{2} \mathrm{ZnSiO}_{4}$ were grown from a $\mathrm{Li}_{2} \mathrm{MoO}_{4}$ solvent by a slow-cooling flux method. They were granular in shape with diameters ranging from 0.1 to 0.5 mm . Weissenberg photographs about $\mathbf{b}$ of all crystals examined showed a double-lattice character, indicating that the crystals were twinned on ( 001 ). Further visual intensity estimations of the double spots gave twin ratios approximately equal to $0 \cdot 6: 0 \cdot 4$ for all the crystals. The photographs also showed monoclinic symmetry with systematic absences $0 k 0$ for $k$ odd and $h 0 l$ for $h+l$ odd, indicating the space group $P 2_{1} / n$. A roughly spherical crystal of diameter 0.2 mm was 0567-7408/79/112678-03\$01.00
selected for the data collection. Cell dimensions and intensity data were measured on a Rigaku four-circle diffractometer with graphite-monochromated Mo Ka radiation. The cell dimensions were determined by a least-squares fit to the setting angles of 25 reflections from the larger of the twin components. Intensities were collected using the $\omega-2 \theta$ scan technique with a scan range of $(1.2+0.5 \tan \theta)^{\circ}$. By using a receiving slit with a large aperture $(5.5 \times 5.5 \mathrm{~mm})$, the intensities of pairs of reflections, $h k l$ and $h \bar{k} \bar{l}$, from the two twin components could be collected at the same time. The measured intensities of 1635 reflections $\left(2 \theta<55^{\circ}\right)$ were averaged to yield a set of 772 symmetrically independent values, $I_{o}(h k l)$, after Lp corrections. No correction was made for absorption.

The intensities $I(h k l)$ and $I(h \bar{k} \bar{l})$ were separated from the observed intensities $I_{o}(h k l)$ and $I_{o}(h \bar{k})$ according to the following equations (Nes \& Vos, 1978):

$$
\begin{aligned}
& I_{o}(h k l)=w_{1} I(h k l)+w_{2} I(h \bar{k} \bar{l}) \\
& I_{o}(h \bar{k} \bar{l})=w_{2} I(h k l)+w_{1} I(h \bar{k} \bar{l}),
\end{aligned}
$$

where $h k l$ refer to the larger of the twin components, and $w_{1} / w_{2}\left(w_{1}+w_{2}=1\right)$ is the twin ratio. The initial set of intensity data was obtained for $w_{1}=0.6$.

A three-dimensional Patterson map revealed positions of the Zn atoms, and the Si and O atoms were located from subsequent Fourier maps. Refinements of © 1979 International Union of Crystallography

Table 1. Final atomic coordinates with their e.s.d.'s

|  | $x$ | $y$ | $z$ |
| :--- | :---: | :--- | :--- |
|  | $y$ | $y$ |  |
| Zn | $0.4986(1)$ | $0.1647(1)$ | $0.3095(1)$ |
| Si | $0.2474(3)$ | $0.4124(2)$ | $0.3135(3)$ |
| $\mathrm{Li}(1)$ | $-0.0088(19)$ | $0.1603(12)$ | $0.3033(12)$ |
| $\mathrm{Li}(2)$ | $0.2381(21)$ | $0.076(12)$ | $0.7157(25)$ |
| $\mathrm{O}(1)$ | $0.2484(8)$ | $0.4092(4)$ | $0.6378(9)$ |
| $\mathrm{O}(2)$ | $0.2551(7)$ | $0.5564(4)$ | $0.2072(9)$ |
| $\mathrm{O}(3)$ | $0.0329(7)$ | $0.3414(4)$ | $0.2033(9)$ |
| $\mathrm{O}(4)$ | $0.4596(7)$ | $0.3387(4)$ | $0.2094(9)$ |

the atomic parameters for various values of $w_{1}(0.55-$ 0.70 ) were carried out by the block-diagonal leastsquares method (HBLS V; Ashida, 1973) with isotropic temperature factors and unit weights. The $R$ value thus obtained was 0.103 for $w_{1}=0 \cdot 64$. A subsequent difference map revealed positions of the remaining Li atoms. Further refinements with isotropic temperature factors for the Li atoms and anisotropic temperature factors for the $\mathrm{Zn}, \mathrm{Si}$ and O atoms gave the final $R$ of 0.060 for $w_{1}=0.65$. Atomic scattering factors for $\mathrm{Zn}^{2+}, \mathrm{Si}^{2} \mathrm{Li}^{+}$and $\mathrm{O}^{-}$were taken from International Tables for X-ray Crystallography (1974). Final positional parameters are given in Table 1.* All computations were made on an ACOS System 800 computer of the Computation Center of Osaka University.

Discussion. Fig. 1 shows the structure viewed along $\mathbf{c}$. The structure is based on a distorted hexagonal-closepacking arrangement of O atoms with layers stacked parallel to ( 001 ). All cations are coordinated tetrahedrally by O atoms. The $\mathrm{ZnO}_{4}$ and $\mathrm{Li}(1) \mathrm{O}_{4}$ tetra-

[^0]

Fig. 1. The crystal structure viewed along $\mathbf{c}$.

Table 2. Selected bond distances $(\AA)$ and angles $\left({ }^{\circ}\right)$

| $\mathrm{SiO}_{4}$ tetrahedron |  | $\mathrm{O}(1)-\mathrm{O}(2)$ |  | $\begin{gathered} \mathrm{O}-\mathrm{M}-\mathrm{O} \\ \text { angles } \end{gathered}$ |
| :---: | :---: | :---: | :---: | :---: |
| $\mathrm{Si}-\mathrm{O}(1)$ | 1.629 (5) |  | 2.667 (7) | 110.5 (3) |
| -O(2) | 1.617 (5) | -O(3) | 2.654 (7) | 109.0 (3) |
| -O(3) | 1.632 (5) | -O(4) | $2 \cdot 643$ (7) | 108.3 (3) |
| -O(4) | 1.632 (5) | $\mathrm{O}(2)-\mathrm{O}(3)$ | $2 \cdot 670$ (6) | $110 \cdot 5$ (3) |
|  |  | -O(4) | 2.639 (6) | 108.6 (3) |
|  |  | $\mathrm{O}(3)-\mathrm{O}(4)$ | 2.672 (6) | 109.9 (2) |
| $\mathrm{ZnO}_{4}$ tetrahedron |  |  |  |  |
| $\mathrm{Zn}-\mathrm{O}$ (1) | 1.956 (5) | $\mathrm{O}(1)-\mathrm{O}(2)$ | 3.274 (7) | 113.4 (2) |
| -O(2) | 1.961 (5) | -O(3) | $3 \cdot 235$ (7) | 110.2 (2) |
| -O(3) | 1.988 (5) | -O(4) | $3 \cdot 212$ (7) | 111.6 (2) |
| -O(4) | 1.927 (5) | $\mathrm{O}(2)-\mathrm{O}(3)$ | 2.934 (6) | 95.0 (2) |
|  |  | -O(4) | 3.310 (6) | 116.7 (2) |
|  |  | $\mathrm{O}(3)-\mathrm{O}(4)$ | $3 \cdot 160$ (6) | 107.6 (2) |
| $\mathrm{Li}(1) \mathrm{O}_{4}$ tetrahedron |  |  |  |  |
| $\mathrm{Li}(1)-\mathrm{O}(1)$ | 1.88 (1) | $\mathrm{O}(1)-\mathrm{O}(2)$ | 3.219 (7) | 115.3 (7) |
| -O(2) | 1.93 (1) | -O(3) | 3.214 (7) | 111.8 (6) |
| -O(3) | 2.00 (1) | -O(4) | 3.237 (7) | 110.9 (6) |
| -O(4) | 2.05 (1) | $\mathrm{O}(2)-\mathrm{O}(3)$ | 3.329 (6) | 115.5 (6) |
|  |  | -O(4) | 2.979 (6) | 96.7 (6) |
|  |  | $\mathrm{O}(3)-\mathrm{O}(4)$ | $3 \cdot 215$ (6) | 105.0 (6) |
| $\mathrm{Li}(2) \mathrm{O}_{4}$ tetrahedron |  |  |  |  |
| $\mathrm{Li}(2)-\mathrm{O}(1)$ | 1.92 (2) | $\mathrm{O}(1)-\mathrm{O}(2)$ | $3 \cdot 257$ (7) | 106.7 (6) |
| -O(2) | $2 \cdot 13$ (2) | -O(3) | $3 \cdot 280$ (7) | 111.6 (6) |
| -O(3) | 2.04 (2) | -O(4) | 3.324 (7) | 117.7 (7) |
| -O(4) | 1.96 (2) | $\mathrm{O}(2)-\mathrm{O}(3)$ | 2.934 (6) | 89.2 (6) |
|  |  | -O(4) | 2.979 (6) | 93.2 (6) |
|  |  | $\mathrm{O}(3)-\mathrm{O}(4)$ | $3 \cdot 590$ (6) | 127.4 (7) |

hedral pairs share corners to form a chain along a, and these chains are held together through other corners, thus forming puckered layers parallel to (010). Similarly the $\mathrm{SiO}_{4}$ and $\mathrm{Li}(2) \mathrm{O}_{4}$ tetrahedral pairs form a chain along a, and these chains also form puckered layers parallel to (010). These two kinds of layers are held together through common corners or edges to form a three-dimensional framework. The same type of framework is seen in the high-temperature form of $\mathrm{Li}_{3} \mathrm{PO}_{4}$ (Zemann, 1960) and in $\mathrm{Zn}-\mathrm{Li}$ silicate ( Yu , Smith \& Austerman, 1978).

Selected bond distances and angles are listed in Table 2. The $\mathrm{SiO}_{4}$ tetrahedra are quite regular with a mean $\mathrm{Si}-\mathrm{O}$ distance of $1.628 \AA$. On the other hand the $\mathrm{ZnO}_{4}$ tetrahedra are significantly distorted. The $\mathrm{Zn}-\mathrm{O}$ distances range from 1.927 (5) to 1.988 (5) $\AA$ with a mean value of $1.958 \AA$ which is normal for a coordination tetrahedron about Zn . The $\mathrm{LiO}_{4}$ tetrahedra also show marked departures from a regular tetrahedron. The $\mathrm{Li}-\mathrm{O}$ distances range from 1.88 (1) to 2.05 (1) $\AA$ for $\mathrm{Li}(1)$ and from 1.92 (2) to 2.13 (2) $\AA$ for $\mathrm{Li}(2)$ with mean values of 1.97 and $2.01 \AA$ respectively. These mean values may be compared with the values of 1.96 and $1.99 \AA$ in $\mathrm{Li}_{3} \mathrm{PO}_{4}$ and 1.959 and $2.009 \AA$ in $\mathrm{Li}_{2} \mathrm{BeSiO}_{4}$ (Howie \& West, 1974) for the corresponding $\mathrm{Li}(1)$ and $\mathrm{Li}(2)$ tetrahedral sites. It is to be noted that the coordination tetrahedra at the $\operatorname{Li}(2)$


Fig. 2. Relative orientations of the twin components at the twin boundary. The twin boundary is shown by the broken line. The fractional $a$ coordinates are shown as percentages of the $a$ length.
sites in the above compounds are all more distorted than those at the $\mathrm{Li}(1)$ sites.

Fig. 2 shows a probable model for twinning. The twin symmetry relating the two twin components is $2_{1}$ parallel to a , by which the arrangements of the $\mathrm{O}, \mathrm{Si}$ and $\mathrm{Li}(2)$ atoms remain almost unchanged since originally they have pseudo $2_{1}$ symmetry. The positions
of the Zn and $\mathrm{Li}(1)$ atoms are also approximately related to each other by 2 , symmetry, and further $\mathrm{Zn}^{2+}$ and $\mathrm{Li}^{+}$ions in fourfold coordination have nearly equal effective ionic radii (Whittaker \& Muntus, 1970). Therefore the $\mathrm{ZnO}_{4}$ and $\mathrm{Li}(1) \mathrm{O}_{4}$ tetrahedra at the twin boundary do not suffer significant distortions.

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# Structure of Cobalt Dilithium Silicate $\beta_{1 \mathrm{II}}-\mathrm{Li}_{2} \mathrm{CoSiO}_{4}$ 

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> Abstract. $\mathrm{Li}_{2} \mathrm{CoSiO}_{4}$, orthorhombic, $P b n 2_{1}, a=$ 6.253 (5), $b=10.685$ (9), $c=4.929$ (9) $\AA$, $Z=4, D_{x}$ $=3.33 \mathrm{Mg} \mathrm{m}^{-3}, \mu($ Mo $K \alpha)=5.50 \mathrm{~mm}^{-1}$. The structure of the $\beta_{\mathrm{II}}$ modification has been solved by the heavy-atom method and refined by the least-squares method to $R=0.044$ for 789 observed reflections. The $\mathrm{Co}^{2+}$ ion is coordinated tetrahedrally by O atoms. The 0567-7408/79/112680-03\$01.00

Co-O distances range from 1.966 (5) to 1.983 (6) $\AA$ with a mean of $1.975 \AA$.

Introduction. Crystals of $\beta_{\mathrm{II}}-\mathrm{Li}_{2} \mathrm{CoSiO}_{4}$ were grown from a LiCl flux (Setoguchi, 1979). They were granular in shape with diameters ranging from 0.3 to 2 mm . Weissenberg photographs of all 17 crystals examined © 1979 International Union of Crystallography


[^0]:    * Lists of structure factors and thermal parameters have been deposited with the British Library Lending Division as Supplementary Publication No. SUP 34640 ( 5 pp .). Copies may be obtained through The Executive Secretary, International Union of Crystallography, 5 Abbey Square, Chester CH1 2HU, England.

